## M.A. DEGREE EXAMINATION - ECONOMICS

FIRST SEMESTER - NOVEMBER 2013
EC 1809 - MATHEMATICS \& STATISTICS FOR ECONOMISTS

Date: 13/11/2013
Time : 1:00-4:00
Dept. No. $\square$ Max. : 100 Marks

> Part - A

Answer any FIVE questions. Each question carries four marks.
( $5 \times 4=20$ )

1. Distinguish between triangular matrix and diagonal matrix.
2. Given the matrices $A=\left[\begin{array}{ll}1 & 2 \\ 3 & 4\end{array}\right]$ and $B=\left[\begin{array}{ll}5 & 6 \\ 7 & 8\end{array}\right]$, Prove that $A B \neq B A$.
3. If $y=\log x^{4}$, find $\frac{d y}{d x}$.
4. Find $\eta$, if price of a commodity is Rs. 8 and MR is Rs. 6.
5. From following information find the correlation between X and Y .
$\sum \mathrm{dxdy}=26, \quad \sum \mathrm{dx}=10, \quad \sum \mathrm{dy}=4, \quad \sum \mathrm{dx}^{2}=62, \quad \sum \mathrm{dy}^{2}=42, \mathrm{~N}=8$.
6. For a Binomial distribution with parameters $\mathrm{n}=5, \mathrm{p}=0.3$ find the probability of getting atleast 3 successes.
7. List out the procedure for Testing Hypothesis.
Part - B

Answer any FOUR questions. Each question carries ten marks. (4 x $10=40$ )
8. Solve the following Linear Equations by using Cramer's Rule.

$$
\begin{aligned}
& 5 x+3 y=65 \\
& 2 y-z=11 \\
& 3 x+4 z=57
\end{aligned}
$$

9. Compute Cofactor for the Matrix $\mathrm{A}=\left[\begin{array}{lll}5 & 2 & 1 \\ 2 & 1 & 4 \\ 0 & 5 & 6\end{array}\right]$ and also prove that $\left|\mathrm{A}^{\mathrm{T}}\right|=|\mathrm{A}|$.
10. (a) Find all the partial derivatives of $z=x^{3}+y^{3}-3 x y$.
(b) Find the total derivative of $z=\left(x^{2}+y\right)\left(2 x-y^{2}\right)$.
11. Compute coefficient of correlation between x and y from the following data.

| $\mathrm{X}:$ | 1 | 3 | 5 | 8 | 9 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{Y}:$ | 3 | 4 | 8 | 10 | 12 | 11 |

12. Compute the average seasonal movement for the following series by the method of simple average

| Year | Jan | Feb | Mar | Apr | May | Jun | Jul | Aug | Sep | Oct | Nov | Dec |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 2006 | 318 | 281 | 278 | 250 | 231 | 216 | 223 | 245 | 269 | 302 | 325 | 347 |
| 2007 | 342 | 309 | 299 | 268 | 249 | 236 | 242 | 262 | 288 | 321 | 342 | 364 |
| 2008 | 367 | 328 | 320 | 287 | 269 | 251 | 259 | 284 | 309 | 345 | 367 | 394 |
| 2009 | 392 | 349 | 342 | 311 | 290 | 273 | 282 | 305 | 328 | 364 | 389 | 417 |

13. Explain the properties of normal distribution.
14. The three samples below have been obtained from normal populations with equal variances. Test the hypothesis that the sample means are equal.

| $\mathrm{X}_{1}$ | $\mathrm{X}_{2}$ | $\mathrm{X}_{3}$ |
| :---: | :---: | :---: |
| 8 | 7 | 12 |
| 10 | 5 | 9 |
| 7 | 10 | 13 |
| 14 | 9 | 12 |
| 11 | 9 | 14 |

The table value of F at $5 \%$ level of significance for $\mathrm{v}_{1}=2$ and $\mathrm{v}_{2}=12$ is 3.88 .

## Part - C

Answer any TWO questions. Each question carries twenty marks. $\quad(2 \times 20=40)$
15. Solve the following set of Linear Simultaneous Equations by using matrix inversion technique.

$$
\begin{align*}
2 x_{1}+4 x_{2}-x_{3} & =15 .  \tag{1}\\
x_{1}-3 x_{2}+2 x_{3} & =-5 .  \tag{2}\\
6 x_{1}+5 x_{2}+x_{3} & =28 . \tag{3}
\end{align*}
$$

16. Given the following Revenue ( R ) and Cost (C) functions for a firm $R=20 q+q^{2}$ and $c=q^{2}+8 q+2$
(a) Find the equilibrium level of output, price at which profit is maximum, and
(b) Find total revenue, total cost at that level of output.
17. Find out the following from given values of X and Y .
(a) The two regression coefficients.
(b) Coefficient of correlation.
(c) Most likely value of X when $\mathrm{Y}=12$.
(d) Most likely value of Y when $\mathrm{X}=22$.

| $\mathrm{X}:$ | 2 | 8 | 10 | -2 | 5 | -4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Y}:$ | 3 | 2 | 5 | 10 | -2 | -3 |

18. Calculate seasonal indices by the ratio to moving average method, from the following data.

| Year | $1^{\text {st }}$ Quarter | $2^{\text {nd }}$ Quarter | $3^{\text {rd }}$ Quarter | $4^{\text {th }}$ Quarter |
| :---: | :---: | :---: | :---: | :---: |
| 2007 | 68 | 62 | 61 | 63 |
| 2008 | 65 | 58 | 66 | 61 |
| 2009 | 68 | 63 | 63 | 67 |

